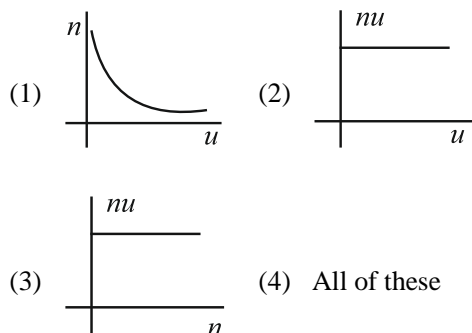


**SECTION - A**

1. Which of the following graph is correct:  
 $n$  = magnitude of measurement &  $u$  = unit of measurement.



2. Choose the wrong statement:  
 (1) A dimensionally correct equation may be correct  
 (2) A dimensionally incorrect equation must be incorrect  
 (3) A dimensionally correct equation may be incorrect  
 (4) A dimensionally incorrect equation may be correct

3. Suppose refractive index  $\mu$  is given as:

$$\mu = A + \frac{B}{\lambda^2}$$

Where A and B are constants and  $\lambda$  is the wavelength, then dimensions of B are same as that of:

- (1) Wavelength (2) Volume  
 (3) Pressure (4) Area

4.  $\alpha = \frac{F}{v^2} \sin(\beta t)$  (where  $v$  = velocity,

$F$  = force,  $t$  = time)

Find the dimension of  $\alpha$  and  $\beta$  respectively

- (1)  $M^1 L^{-1} T^0, M^1 L^{-1} T^0$   
 (2)  $M^1 L^1 T^{-2}, M^1 L^{-1} T^0$   
 (3)  $M^{-1} L^{-1} T^{-2}, M^1 L^1 T^{-2}$   
 (4)  $M^1 L^{-1} T^0, M^0 L^0 T^{-1}$

5. Which of the following have unit but does not have dimension?

- (1) Strain (2) Speed  
 (3) Angle (4) Height

6. Vander Waal's gas equation is

$$\left(P + \frac{a}{V^2}\right)(V-b) = RT. \text{ The dimensions of constant}$$

a as given above are

- (1)  $ML^4 T^{-2}$  (2)  $ML^5 T^{-2}$   
 (3)  $ML^3 T^{-2}$  (4)  $ML^2 T^{-2}$

7. If a particle moves from point P (2, 3, 5) to point Q (3, 4, 5). Its displacement vector be

- (1)  $\hat{i} + \hat{j} + 10\hat{k}$  (2)  $\hat{i} + \hat{j} + 5\hat{k}$   
 (3)  $\hat{i} + \hat{j}$  (4)  $2\hat{i} + 4\hat{j} + 6\hat{k}$

8. The angles which a vector  $\hat{i} + \hat{j} + \sqrt{2}\hat{k}$  make with X, Y and Z axes respectively are

- (1)  $60^\circ, 60^\circ, 60^\circ$  (2)  $45^\circ, 45^\circ, 45^\circ$   
 (3)  $60^\circ, 60^\circ, 45^\circ$  (4)  $45^\circ, 45^\circ, 60^\circ$

9. If  $\vec{A} \times \vec{B} = \vec{B} \times \vec{A}$ , then the angle between  $\vec{A}$  and  $\vec{B}$  is

- (1)  $\frac{\pi}{2}$  (2)  $\frac{\pi}{3}$   
 (3)  $\pi$  (4)  $\frac{\pi}{4}$

10. If a vector  $\vec{P}$  making angles  $\alpha, \beta$  and  $\gamma$  respectively with X, Y and Z axes respectively.

Then  $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma =$

- (1) 0 (2) 1  
 (3) 2 (4) 3

11. The angle between the two vectors  $\vec{A} = 3\hat{i} + 4\hat{j} + 5\hat{k}$  and  $\vec{B} = 3\hat{i} + 4\hat{j} - 5\hat{k}$  will be

- (1)  $90^\circ$   
 (2)  $0^\circ$   
 (3)  $60^\circ$   
 (4)  $45^\circ$

12. The unit vector along  $\hat{i} - 2\hat{j}$  is :

- (1)  $\frac{\hat{i} - 2\hat{j}}{\sqrt{5}}$  (2)  $\hat{i} + \hat{j}$   
 (3)  $\frac{\hat{i} + \hat{j}}{\sqrt{2}}$  (4)  $\frac{\hat{i} - \hat{j}}{\sqrt{5}}$

13. If a unit vector is represented by  $0.3\hat{i} - 0.4\hat{j} + c\hat{k}$ , then the value of 'c' is :

- (1)  $\sqrt{0.75}$   
 (2)  $\sqrt{0.25}$   
 (3)  $\sqrt{0.01}$   
 (4)  $\sqrt{0.39}$

14. Forces 7 N, 24 N, 25 N act at a point in mutually perpendicular directions. The magnitude of the resultant force is :

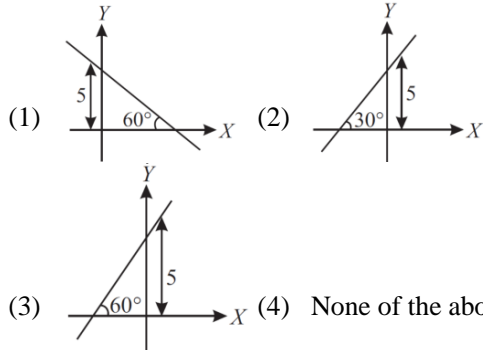
- (1) 19 N (2) 13 N  
 (3) 26 N (4)  $25\sqrt{2}$  N

15. A physical quantity  $A$  is related to four observable  $a, b, c$  and  $d$  as follows,  $A = \frac{a^2 b^3}{c \sqrt{d}}$ , the percentage errors of measurement in  $a, b, c$  and  $d$  are 1%, 3%, 2% and 2% respectively. What is the percentage error in the quantity  $A$
- (1) 12% (2) 7%  
(3) 5% (4) 14%
16. If  $\vec{P} \cdot \vec{Q} = -PQ$ , then angle between  $\vec{P}$  and  $\vec{Q}$  is :
- (1)  $0^\circ$  (2)  $180^\circ$   
(3)  $45^\circ$  (4)  $60^\circ$
17. A dimensionless quantity
- (1) Never has a unit (2) Always has a unit  
(3) May have a unit (4) Does not exist
18. A unitless quantity
- (1) Does not exist  
(2) Always has a nonzero dimension  
(3) Never has a nonzero dimension  
(4) May have a nonzero dimension
19. If  $S = 1/3 \text{ ft}^3$ ,  $f$  has the dimensions of ( $S = \text{distance}, t = \text{time}$ )
- (1)  $[M^0 L^{-1} T^3]$  (2)  $[M^1 L^1 T^{-3}]$   
(3)  $[M^0 L^1 T^{-3}]$  (4)  $[M^0 L^{-1} T^{-3}]$
20. For  $e^{(at+3)}$ , the dimensions of  $a$  is:
- (1)  $M^0 L^0 T^0$  (2)  $M^0 L^0 T^1$   
(3)  $M^0 L^0 T^{-1}$  (4) None of these
21. The velocity  $u$  of particles is given in terms of time  $t$  by the equation  $u = at + \frac{b}{t^2 + c}$ .
- The dimension of  $a, b$  and  $c$  are:
- (1)  $L^2, T, LT^2$  (2)  $LT^2, LT, L$   
(3)  $LT^{-2}, LT, T^2$  (4)  $L, LT, T^2$
22. The angle between the vectors  $\vec{A}$  and  $\vec{B}$  is  $\theta$ . The value of the triple product  $\vec{A} \cdot (\vec{B} \times \vec{A})$  is
- (1)  $A^2 B$   
(2) Zero  
(3)  $A^2 B \sin \theta$   
(4)  $A^2 B \cos \theta$
23. If two vectors  $2\hat{i} + 3\hat{j} - \hat{k}$  and  $-4\hat{i} - 6\hat{j} - \lambda\hat{k}$  are parallel to each other then value of  $\lambda$  be
- (1) 0 (2) -2  
(3) 3 (4) 4
24. If velocity  $v$ , acceleration  $A$  and force  $F$  are chosen as fundamental quantities, then the dimensional formula of angular momentum in terms of  $v, A$  and  $F$  would be
- (1)  $FA^{-1}v$  (2)  $Fv^3 A^{-2}$   
(3)  $Fv^2 A^{-1}$  (4)  $F^2 v^2 A^{-1}$

25. In the following list, the only pair which have different dimensions, is
- (1) Linear momentum and moment of a force  
(2) Planck's constant and angular momentum  
(3) Pressure and modulus of elasticity  
(4) Torque and potential energy
26. In an clockwise system
- (1)  $\hat{j} \times \hat{k} = \hat{i}$  (2)  $\hat{i} \cdot \hat{i} = 0$   
(3)  $\hat{j} \times \hat{j} = 1$  (4)  $\hat{k} \cdot \hat{j} = 1$
27. The linear velocity of a rotating body is given by  $\vec{v} = \vec{\omega} \times \vec{r}$ , where  $\vec{\omega}$  is the angular velocity and  $\vec{r}$  is the radius vector. The angular velocity of a body is  $\vec{\omega} = \hat{i} - 2\hat{j} + 2\hat{k}$  and the radius vector  $\vec{r} = 4\hat{j} - 3\hat{k}$ , then  $|\vec{v}|$  is
- (1)  $\sqrt{29}$  units (2)  $\sqrt{31}$  units  
(3)  $\sqrt{37}$  units (4)  $\sqrt{41}$  units
28. Three vectors  $\vec{a}, \vec{b}$  and  $\vec{c}$  satisfy the relation  $\vec{a} \cdot \vec{b} = 0$  and  $\vec{a} \cdot \vec{c} = 0$ . The vector  $\vec{a}$  is parallel to
- (1)  $\vec{b}$  (2)  $\vec{c}$   
(3)  $\vec{b} \cdot \vec{c}$  (4)  $\vec{b} \times \vec{c}$
29. The diagonals of a parallelogram are  $2\hat{i}$  and  $2\hat{j}$ . What is the area of the parallelogram
- (1) 0.5 units (2) 1 unit  
(3) 2 units (4) 4 units
30. What is the unit vector perpendicular to the following vectors  $2\hat{i} + 2\hat{j} - \hat{k}$  and  $6\hat{i} - 3\hat{j} + 2\hat{k}$
- (1)  $\frac{\hat{i} + 10\hat{j} - 18\hat{k}}{5\sqrt{17}}$  (2)  $\frac{\hat{i} - 10\hat{j} + 18\hat{k}}{5\sqrt{17}}$   
(3)  $\frac{\hat{i} - 10\hat{j} - 18\hat{k}}{5\sqrt{17}}$  (4)  $\frac{\hat{i} + 10\hat{j} + 18\hat{k}}{5\sqrt{17}}$
31.  $\cos 150^\circ$
- (1)  $\frac{1}{2}$  (2)  $-\frac{1}{2}$   
(3)  $\frac{\sqrt{3}}{2}$  (4)  $-\frac{\sqrt{3}}{2}$
32. If  $\sin \theta = \cos \theta$ , then the value of  $\theta$  will be:
- (1)  $0^\circ$  (2)  $45^\circ$   
(3)  $30^\circ$  (4)  $90^\circ$
33. Given that,  $\sin A = \frac{1}{2}$  and  $\cos B = \frac{1}{\sqrt{2}}$  then value of  $(A + B)$  will be:
- (1)  $30^\circ$  (2)  $45^\circ$   
(3)  $75^\circ$  (4)  $15^\circ$

34. What is the value of linear velocity, if  $\vec{\omega} = 3\hat{i} - 4\hat{j} + \hat{k}$  and  $\vec{r} = 5\hat{i} - 6\hat{j} + 6\hat{k}$
- (1)  $6\hat{i} - 2\hat{j} + 3\hat{k}$  (2)  $6\hat{i} - 2\hat{j} + 8\hat{k}$   
 (3)  $4\hat{i} - 13\hat{j} + 6\hat{k}$  (4)  $-18\hat{i} - 13\hat{j} + 2\hat{k}$

35. Plot the graph of given equation,  $Y = \sqrt{3}X + 5$



- (3) (4) None of the above

### SECTION - B

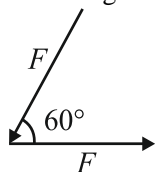
36. If a vector  $2\hat{i} + 3\hat{j} + 8\hat{k}$  is perpendicular to the vector  $4\hat{i} - 4\hat{j} + \alpha\hat{k}$ , then the value of  $\alpha$  is
- (1)  $-1$  (2)  $\frac{1}{2}$   
 (3)  $-\frac{1}{2}$  (4)  $1$

37. If  $|\vec{A} \times \vec{B}| = \sqrt{3}\vec{A} \cdot \vec{B}$ , then the value of  $|\vec{A} + \vec{B}|$  is:

- (1)  $\left(A^2 + B^2 + \frac{AB}{\sqrt{3}}\right)^{1/2}$   
 (2)  $A + B$   
 (3)  $\left(A^2 + B^2 + \sqrt{3}AB\right)^{1/2}$   
 (4)  $\left(A^2 + B^2 + AB\right)^{1/2}$

38. If the magnitudes of vectors  $\vec{A}$ ,  $\vec{B}$  and  $\vec{C}$  are 12, 5, and 13 units respectively and  $\vec{A} + \vec{B} = \vec{C}$ , the angle between vectors  $A$  and  $B$  is:
- (1)  $0$  (2)  $\pi$   
 (3)  $\frac{\pi}{2}$  (4)  $\frac{\pi}{4}$

39. Two forces, each numerically equal to 5 N, are acting as shown in the figure. Then the resultant is



- (1) 2.5 N (2) 5 N  
 (3)  $5\sqrt{3}$  N (4) 10 N

40. Unit of power is  
 (1) Kilowatt (2) Kilowatt-hour  
 (3) Dyne (4) Joule

41. The dimensional formula for impulse is  
 (1)  $MLT^{-2}$  (2)  $MLT^{-1}$   
 (3)  $ML^2T^{-1}$  (4)  $M^2LT^{-1}$

42. The dimensional formula for Planck's constant ( $h$ ) is  
 (1)  $ML^{-2}T^{-3}$  (2)  $ML^2T^{-2}$   
 (3)  $ML^2T^{-1}$  (4)  $ML^{-2}T^{-2}$

43. The dimensional formula for Boltzmann's constant is  
 (1)  $[ML^2T^{-2}\theta^{-1}]$  (2)  $[ML^2T^{-2}]$   
 (3)  $[ML^0T^{-2}\theta^{-1}]$  (4)  $[ML^{-2}T^{-1}\theta^{-1}]$

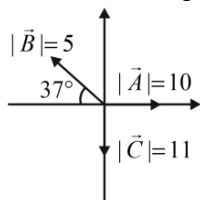
44. Let  $\vec{C} = \vec{A} + \vec{B}$  then  
 (1)  $|\vec{C}|$  is always greater than  $|\vec{A}|$   
 (2) It is possible to have  $|\vec{C}| < |\vec{A}|$  and  $|\vec{C}| < |\vec{B}|$   
 (3)  $C$  is always equal to  $A + B$   
 (4)  $C$  is never equal to  $A + B$

45. A force  $\vec{F} = (5\hat{i} + 3\hat{j})$  Newton is applied over a particle which displaces it from its origin to the point  $\vec{r} = (2\hat{i} - 1\hat{j})$  metres. The work done on the particle is  
 (1)  $-7 J$  (2)  $+13 J$   
 (3)  $+7 J$  (4)  $+11 J$

46. If the sum of two unit vectors is a unit vector, then magnitude of difference is  
 (1)  $\sqrt{2}$  (2)  $\sqrt{3}$   
 (3)  $\frac{1}{\sqrt{2}}$  (4)  $\sqrt{5}$

47. The vectors from origin to the points  $A$  and  $B$  are  $\vec{A} = 3\hat{i} - 6\hat{j} + 2\hat{k}$  and  $\vec{B} = 2\hat{i} + \hat{j} - 2\hat{k}$  respectively. The area of the triangle  $OAB$  be  
 (1)  $\frac{5}{2}\sqrt{17}$  sq. units  
 (2)  $\frac{2}{5}\sqrt{17}$  sq. units  
 (3)  $\frac{3}{5}\sqrt{17}$  sq. units  
 (4)  $\frac{5}{3}\sqrt{17}$  sq. units

48. Find the resultant of following vectors



- (1) 8  
(3) 10  
(2) 6  
(4) 20
49. The frequency of vibration  $f$  of a mass  $m$  suspended from a spring of spring constant  $K$  is given by a relation of this type  $f = C m^x K^y$ ; where  $C$  is a dimensionless quantity. The value of  $x$  and  $y$  are

- (1)  $x = \frac{1}{2}, y = \frac{1}{2}$   
(3)  $x = \frac{1}{2}, y = -\frac{1}{2}$   
(2)  $x = -\frac{1}{2}, y = -\frac{1}{2}$   
(4)  $x = -\frac{1}{2}, y = \frac{1}{2}$

50. The velocity of water waves  $v$  may depend upon their wavelength  $\lambda$ , the density of water  $\rho$  and the acceleration due to gravity  $g$ . The method of dimensions gives the relation between these quantities as

- (1)  $v^2 \propto g$   
(3)  $v^2 \propto g\lambda$   
(2)  $v^2 \propto g\lambda\rho$   
(3)  $v^2 \propto g^{-1}\lambda^{-3}$

## Solution

1. (4)  
Relation between unit and magnitude  
( $nu = \text{constant}$ ).
2. (4)  
A dimensionally incorrect equation may be correct.
3. (4)  
 $\lambda = \text{wavelength}$   
 $[\lambda] = L$   
 $\mu = (A) + \left(\frac{B}{\lambda^2}\right) \Rightarrow \left[\frac{B}{\lambda^2}\right] = M^0 L^0 T^0$   
 $[B] = M^0 L^2 T^0$   
B = S.I. unit ( $m^2$ )
4. (4)  
 $\alpha = \frac{F}{v^2} \sin(\beta t)$   
dimensionless      dimensionless  
So  $\alpha = \frac{[F]}{[v^2]} = \frac{[M^1 L^1 T^{-2}]}{[L^1 T^{-1}]^2} = M^1 L^{-1} T^0$   
 $\beta = \frac{1}{[t]} = \frac{1}{[T]} = M^0 L^0 T^{-1}$
5. (3)  
 $\theta = \frac{l}{r} = \frac{[L]}{[L]} = [M^0 L^0 T^0]$   
and the S.I unit of angle is radian
6. (2)  
 $P \rightarrow \text{Pressure}$   
 $V \rightarrow \text{Volume}$   
 $T \rightarrow \text{Temperature}$   
 $R \rightarrow \text{const}$   
 $P = \frac{a}{V^2} \Rightarrow ML^{-1} T^{-2} = \frac{a}{(L^3)^2}$   
 $a = ML^{-1} T^{-2} L^6 = [M^1 L^5 T^{-2}]$
7. (3)  
Displacement vector  $\vec{r} = \Delta x \hat{i} + \Delta y \hat{j} + \Delta z \hat{k}$   
 $= (3-2)\hat{i} + (4-3)\hat{j} + (5-5)\hat{k} = \hat{i} + \hat{j}$
8. (3)  
 $\vec{R} = \hat{i} + \hat{j} + \sqrt{2}\hat{k}$   
Comparing the given vector with  
 $R = R_x \hat{i} + R_y \hat{j} + R_z \hat{k}$   
 $R_x = 1, R_y = 1, R_z = \sqrt{2}$   
and  $|\vec{R}| = \sqrt{R_x^2 + R_y^2 + R_z^2} = 2$

- $$\cos \alpha = \frac{R_x}{R} = \frac{1}{2} \Rightarrow \alpha = 60^\circ$$
- $$\cos \beta = \frac{R_y}{R} = \frac{1}{2} \Rightarrow \beta = 60^\circ$$
- $$\cos \gamma = \frac{R_z}{R} = \frac{1}{\sqrt{2}} \Rightarrow \gamma = 45^\circ$$
9. (3)  
We know that  $\vec{A} \times \vec{B} = -(\vec{B} \times \vec{A})$  because the angle between these two is always  $90^\circ$ .  
But if the angle between  $\vec{A}$  and  $\vec{B}$  is 0 or  $\pi$ . Then  $\vec{A} \times \vec{B} = \vec{B} \times \vec{A} = 0$ .
  10. (3)  
 $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma$   
 $= 1 - \cos^2 \alpha + 1 - \cos^2 \beta + 1 - \cos^2 \gamma$   
 $= 3 - (\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma) = 3 - 1 = 2$
  11. (1)  
 $\cos \theta = \frac{\vec{A} \cdot \vec{B}}{|\vec{A}| |\vec{B}|} = \frac{(3\hat{i} + 4\hat{j} + 5\hat{k}) \cdot (3\hat{i} + 4\hat{j} - 5\hat{k})}{\sqrt{9+16+25} \sqrt{9+16+25}}$   
 $= \frac{9+16-25}{50} = 0$   
 $\Rightarrow \cos \theta = 0, \therefore \theta = 90^\circ$
  12. (1)
  13. (1)
  14. (4)
  15. (4)  
Percentage error in A  
 $= \left( 2 \times 1 + 3 \times 3 + 1 \times 2 + \frac{1}{2} \times 2 \right) \% = 14\%$
  16. (2)
  17. (3)
  18. (3)
  19. (3)
  20. (3)
  21. (3)  
 $[a] = [LT^{-2}]$   
 $[b] = [LT]$   
 $[c] = [T^2]$   
 $[u] = [LT^{-1}]$   
 $[a][T] = [LT^{-1}]$   
 $[a] = [LT^{-2}]$

22. (2)

23. (2)

Let  $\vec{A} = 2\hat{i} + 3\hat{j} - \hat{k}$  and  $\vec{B} = -4\hat{i} - 6\hat{j} - \lambda\hat{k}$

$\vec{A}$  and  $\vec{B}$  are parallel to each other

$$\frac{a_1}{b_1} = \frac{a_2}{b_2} = \frac{a_3}{b_3} \text{ i.e. } \frac{2}{-4} = \frac{3}{-6} = \frac{-1}{-\lambda} \Rightarrow \lambda = -2.$$

24. (2)

$$L \propto v^x A^y F^z \Rightarrow L = kv^x A^y F^z$$

Putting the dimensions in the above relation

$$[ML^2T^{-1}] = k[LT^{-1}]^x [LT^{-2}]^y [MLT^{-2}]^z$$

$$\Rightarrow [ML^2T^{-1}] = k[M^z L^{x+y+z} T^{-x-2y-2z}]$$

Comparing the powers of  $M, L$  and  $T$

$$z = 1 \quad \dots(i)$$

$$x + y + z = 2 \quad \dots(ii)$$

$$-x - 2y - 2z = -1 \quad \dots(iii)$$

On solving (i), (ii) and (iii)  $x = 3, y = -2, z = 1$

So dimension of  $L$  in terms of  $v, A$  and  $f$

$$[L] = [Fv^3 A^{-2}]$$

25. (1)

Linear momentum = Mass  $\times$  Velocity

$$= [MLT^{-1}]$$

Moment of a force = Force  $\times$  Distance

$$= [ML^2T^{-2}]$$

26. (1)

27. (1)

$$\vec{v} = \vec{\omega} \times \vec{r} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -2 & 2 \\ 0 & 4 & -3 \end{vmatrix} = \hat{i}(6-8) - \hat{j}(-3) + 4\hat{k}$$

$$-2\hat{i} + 3\hat{j} + 4\hat{k}$$

$$|\vec{v}| = \sqrt{(-2)^2 + (3)^2 + 4^2} = \sqrt{29} \text{ unit}$$

28. (4)

$\vec{a} \cdot \vec{b} = 0$  i.e.  $\vec{a}$  and  $\vec{b}$  will be perpendicular to each other

$\vec{a} \cdot \vec{c} = 0$  i.e.  $\vec{a}$  and  $\vec{c}$  will be perpendicular to each other

$\vec{b} \times \vec{c}$  will be a vector perpendicular to both  $\vec{b}$  and  $\vec{c}$

So,  $\vec{a}$  is parallel to  $\vec{b} \times \vec{c}$

29. (3)

$$\text{Area} = \frac{|2\hat{i} \times 2\hat{j}|}{2} = \frac{|4\hat{k}|}{2} = 2 \text{ unit.}$$

$$\vec{B} = \hat{i} - \hat{j} + \hat{k}$$

$$\vec{C} = \vec{A} \times \vec{B} = (2\hat{i} + 2\hat{j} - \hat{k}) \times (6\hat{i} - 3\hat{j} + 2\hat{k})$$

$$= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 2 & -1 \\ 6 & -3 & 2 \end{vmatrix} = \hat{i} - 10\hat{j} - 18\hat{k}$$

Unit vector perpendicular to both  $\vec{A}$  and  $\vec{B}$

$$= \frac{\hat{i} - 10\hat{j} - 18\hat{k}}{\sqrt{1^2 + 10^2 + 18^2}} = \frac{\hat{i} - 10\hat{j} - 18\hat{k}}{5\sqrt{17}}$$

31. (4)

32. (2)

33. (3)

34. (4)

$$\vec{v} = \vec{\omega} \times \vec{r} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & -4 & 1 \\ 5 & -6 & 6 \end{vmatrix} = -18\hat{i} - 13\hat{j} + 2\hat{k}$$

35. (3)

36. (2)

37. (4)

$$|\vec{A} \times \vec{B}| = \sqrt{3} \vec{A} \cdot \vec{B}$$

$$AB \sin \theta = \sqrt{3} AB \cos \theta$$

$$\tan \theta = \sqrt{3}$$

$$\theta = 60^\circ, \text{ then}$$

$$R = (A^2 + B^2 + 2AB \cos 60^\circ)^{1/2}$$

$$= (A^2 + B^2 + AB)^{1/2}$$

38. (3)

$$\vec{C} = \vec{A} + \vec{B}$$

$$|\vec{C}| = |\vec{A} + \vec{B}|$$

$$C^2 = A^2 + B^2 + 2AB \cos \theta$$

$$13^2 = 12^2 + 5^2 + 2 \times 12 \times 5 \cos \theta$$

$$169 = 144 + 25 + 120 \cos \theta$$

$$\theta = \frac{\pi}{2}$$

39. (2)

40. (1)

41. (2)

Impulse = Force  $\times$  Time =

$$[MLT^{-2}][T] = [MLT^{-1}]$$

42. (3)

$$E = hv \Rightarrow [ML^2T^{-2}] = [h][T^{-1}] \Rightarrow [h] = [ML^2T^{-1}]$$

43. (1)

$$k = \left[ \frac{R}{N} \right] = [ML^2T^{-2}\theta^{-1}]$$

44. (2)

45. (3)

$$W = \vec{F} \cdot \vec{r} = (5\hat{i} + 3\hat{j})(2\hat{i} - \hat{j}) = 10 - 3 = 7 J.$$

46. (2)

Let  $n_1$  and  $n_2$  are the two unit vectors, then the sum is

$$\vec{n}_s = n_1 + n_2 \text{ or } n_s^2 = n_1^2 + n_2^2 + 2n_1n_2 \cos \theta$$

Since it is given that  $n_s$  is also a unit vector, therefore

$$1 = 1 + 1 + 2 \cos \theta \Rightarrow \cos \theta = -\frac{1}{2} \therefore \theta = 120^\circ$$

Now the difference vector is

$$n_d = n_1 - n_2 \text{ or } n_d^2 = n_1^2 + n_2^2 - 2n_1n_2 \cos \theta \\ = 1 + 1 - 2 \cos 120^\circ$$

$$\therefore n_d^2 = 2 - 2\left(-\frac{1}{2}\right) = 2 + 1 = 3$$

$$\Rightarrow n_d = \sqrt{3}$$

47. (1)

Given  $\vec{OA} = \vec{a} = 3\hat{i} - 6\hat{j} + 2\hat{k}$  and

$$\vec{OB} = \vec{b} = 2\hat{i} + \hat{j} - 2\hat{k}$$

$$\therefore (\vec{a} \times \vec{b}) = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & -6 & 2 \\ 2 & 1 & -2 \end{vmatrix}$$

$$= (12 - 2)\hat{i} + (4 + 6)\hat{j} + (3 + 12)\hat{k}$$

$$= 10\hat{i} + 10\hat{j} + 15\hat{k} \Rightarrow |\vec{a} \times \vec{b}| = \sqrt{10^2 + 10^2 + 15^2}$$

$$= \sqrt{425} = 5\sqrt{17}$$

$$\text{Area of } \Delta OAB = \frac{1}{2} |\vec{a} \times \vec{b}| = \frac{5\sqrt{17}}{2} \text{ sq. units}$$

48. (3)

49. (4)

By putting the dimensions of each quantity both the sides we get  $[T^{-1}] = [M]^x [MT^{-2}]^y$

Now, comparing the dimensions of quantities in both sides we get  $x + y = 0$  and  $2y = 1 \therefore$

$$x = -\frac{1}{2}, y = \frac{1}{2}$$

50. (3)

Let  $v = k g^y \lambda^z \rho^\delta$ . Now by substituting the dimensions of each quantities and equating the powers of  $M$ ,  $L$  and  $T$  we get  $\delta = 0$  and

$$y = \frac{1}{2}, z = \frac{1}{2}.$$